# Electron-Transfer Reactions: AM1 and ab Initio Studies on Self-Exchange in $p$-Diaminobenzene Systems 

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#### Abstract

AM1 and $\mathrm{HF} / 6-31 \mathrm{G}^{*}$ molecular orbital calculations have been used to investigate the electron self-exchange reactions between a series of substituted 1,4 -diaminobenzenes and their radical cations. Comparisons with known experimental data and the results of the ab initio calculations suggest that AM1 performs well for this problem. The internal reorganization energy, $\lambda_{i}$, has been estimated from the differences between the vertical and adiabatic ionization potentials of the neutral compounds and the corresponding electron affinities of the radical cations and is found to be significantly larger than previous estimates. Direct CI calculations of $\lambda$ for the radical cation/neutral molecule complex reveal that stabilization of the ground state (complexation) and the corresponding destabilization of the first excited state increase $\lambda$ further. There is, however, a large zero-point energy contribution that lowers the classical electrontransfer activation energy significantly. The calculated thermodynamics of the classical activation process are in good agreement with experiment.


Electron-transfer reactions are being increasingly recognized as integral components of many organic reaction mechanisms. There are, however, many indications ${ }^{1}$ that organic electron transfer differs significantly from its inorganic counterparts. Classical Marcus theory ${ }^{2-5}$ has often been applied to inorganic systems with success, ${ }^{6,7}$ but many of its basic assumptions may not be valid for closely coupled organic electron-transfer reactions. ${ }^{1,8-11}$ It is, for instance, becoming increasingly clear that inner reorganization energy, $\lambda_{\mathrm{i}}$, is the major contributor to the activation energy for electron transfer in some organic systems. ${ }^{12,13}$ Molecular orbital calculations, which have been used sparingly for inorganic ${ }^{7,14-16}$ and organic ${ }^{8,17-19}$ systems, are in principle capable of providing reliable values for many of the

[^0]principal variables necessary to obtain the electron-transfer rate constant from Marcus theory. Most applications of MO theory have concentrated on the electronic matrix coupling element, $V_{12}$ (often called $V_{A B}, H_{12}, \ldots$ ), ${ }^{7,14-16,17 \text { a }}$ or on the inner reorganization energy, $\lambda_{\mathrm{i}} \cdot{ }^{12 \mathrm{a}, 20}$

The present study has two principal objectives: to assess the reliability of standard AM1 semiempirical MO theory ${ }^{21}$ for organic electron-transfer reactions and to investigate a reaction system that is far from the loosely coupled outer sphere systems for which Marcus theory is best suited.

The systems investigated are the (Ar:Ar ${ }^{\circ+} \rightarrow \mathrm{Ar}^{\circ+}{ }^{+}: \mathrm{Ar}^{1+} \rightarrow$ $\mathrm{Ar}^{++}$: Ar) self-exchange reactions, where Ar symbolizes the arenes 1,4-diaminobenzene (1), 1-amino-4-(dimethylamino)benzene (2), 1,4-bis(dimethylamino)benzene (3), and 1,4-diamino-2,3,5,6tetramethylbenzene (4). These systems have been investigated extensively in solution, ${ }^{12,13,22,23}$ so that they present many opportunities to compare calculated data with the corresponding values derived from Marcus-theory-based interpretations of experimental data. We have deliberately chosen to investigate the closely coupled reaction occurring within the relatively stable $\mathrm{Ar}^{\circ+}: \mathrm{Ar}$ complexes in order to identify the major differences between such systems and classical loosely coupled electron transfer. Nelsen et al. ${ }^{12}$ have previously investigated 3 using AM1, and Goez ${ }^{20}$ has used AM1-calculated frequencies to estimate $\lambda_{i}$ for 2 and 3.

[^1]Table I: AM1-Calculated and Experimental Molecular Data for 1-4

| system | $\Delta H_{f}^{\text {calc }}$ ( $\mathrm{kcal} / \mathrm{mol}$ ) | $\Delta H_{\mathrm{f}}^{\exp }(\mathrm{kcal} / \mathrm{mol})$ | $\mathrm{IP}_{\text {vert }}^{\text {calc }}(\mathrm{eV})$ | $\mathrm{IP}_{\text {adiab }}^{\text {calc }}$ | IP ${ }^{\text {exp }} a(\mathrm{eV})$ | $\nu_{\pi \rightarrow \pi^{*}}^{\text {calc }}$ (nm) | $\nu_{\pi \rightarrow \pi^{*}}^{\exp }(\mathrm{nm})$ | ZPE (kcal/mol) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 19.99 | 25.5 | 7.64 | 6.53 | 7.51 | 311.8 | 314.9 | 86.19 |
| 2 | 30.14 |  | 7.64 | 6.87 | 7.10 | 319.4 | 315.9 | 121.15 |
| 3 | 40.49 |  | 7.63 | 6.75 | 6.80 | 323.9 | 322.6 | 156.13 |
| 4 | -1.01 |  | 7.34 | 6.75 | 7.00 | 434.2 | 454.6 | 157.52 |
| $1^{+}$ | 181.4 |  |  |  |  |  |  |  |
| $2^{+\bullet}$ | 188.5 |  |  |  |  |  |  |  |
| $3^{+}$ | 196.1 |  |  |  |  |  |  |  |
| $4^{+}$ | 154.6 |  |  |  |  |  |  |  |

${ }^{a}$ Taken from ref 17.
Table II: HF and MP2 Total Energies (au), Zero-Point Energies (kcal mol ${ }^{-1}$ ), and Ionization Potentials (eV)

| species | $\mathrm{PG}^{\text {a }}$ | energy |  | ZPE | IP |  | IP ${ }^{\text {exp }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | HF | MP2 |  | HF | MP2 |  |
| 1 | $C_{2 h}$ | -340.754 53 | -341.83812 | 89.9 | 5.43 | 6.23 | 7.51 |
|  | $C_{20}$ | -340.75432 | -341.83788 | 90.0 | 5.42 | 6.23 | 7.51 |
| $1^{+}$ | $D_{2 h}$ | -340.55507 | -341.609 27 | 90.5 |  |  |  |

${ }^{a}$ Molecular point group.

## Methods

All AMl calculations used the VAMP program (version 4.4), ${ }^{24}$ which is similar to the QCPE programs MOPAC ${ }^{25}$ and AMPAC ${ }^{26}$ but contains an extended CI section, a modified version of Baker's eigenvector following (EF) geometry optimizer, ${ }^{27}$ and has been extensively modified to take advantage of vector computer architecture. The calculations were carried out on a Convex C220/256 and a Cray YMP-432.

All AM1 geometries were optimized until the gradient norm was less than $0.4 \mathrm{kcal}^{-1}$. Gradients were calculated by standard finite difference techniques, where necessary using full SCF calculations a every geometry. Standard AM1 parameters were used throughout. The neutral structures 1-4 were calculated at the RHF level. The half-electron formalism of Dewar et al. ${ }^{28}$ was used for radical cations $1 \mathbf{1 a - 4}$. The reference wave function for the transition states $1 \mathbf{c}-\mathbf{4 c}$ used three electrons distributed evenly over the highest two MOs (i.e. 1.5 electrons per orbital). Unrestricted Hartree-Fock (UHF) theory proved to be unsuitable for the transition-state calculations because the wave function did not reflect the full symmetry of the molecular structure. UHF was used for the $a b$ initio calculations on these transition states, but in this case the wave function was forced to remain symmetrical. This also led to considerable SCF-convergence problems that were less severe in half-electron calculations. Convergence was often obtained using Pulay's DIIS technique. ${ }^{29}$ Our present semiempirical program cannot restrict the symmetry of UHF wave functions, but as the half-electron wave function remains symmetrical, the latter method was used.

The energetic difference between the ground state and the first excited state ( $2 \times V_{12}$ ) and the vertical $\pi \rightarrow \pi^{*}$ excitations of the UV spectra were calculated on the RHF-optimized structures using configuration interaction. The CI expansion ${ }^{30}$ used includes all possible single and double excitations of seven electrons in eight MOs (CISD $=8$, i.e. 338 configurations). This gives reliable vertical excitation energies for many organic systems. ${ }^{31}$
$A b$ initio calculations used the Convex and Cray versions of Gaussian 90. ${ }^{32}$ All calculations used the $6-31 \mathrm{G}^{* 33}$ basis set. Optimizations were carried out using restricted (RHF) and unrestricted Hartree-Fock (UHF) theory for closed- and open-shell systems, respectively. Single-point calculations on the Hartree-Fock geometries included a second-order Møller-Plesset correction (MP2) ${ }^{34}$ for electron correlation within the frozen core approximation. Energies quoted are the projected MP2 ${ }^{35}$

[^2]values for open-shell species. All calculations used direct-SCF and postSCF techniques.

## Results

Ground-State Monomers. The AM1-calculated energetic and electron data for 1-4 are shown in Table I, and the ab initio data, in Table II. As expected for $\mathrm{C}, \mathrm{H}, \mathrm{N}$-containing molecules, the calculated AM1 structures (shown in Chart I) are in good agreement with experimental (X-ray) data. ${ }^{36}$ The most significant differences between the neutral structure and the corresponding radical cation are the decrease in the $\mathrm{C}-\mathrm{N}$ bond length and the change of the nitrogen atom from an $\mathrm{sp}^{3}$ to an $\mathrm{sp}^{2}$ geometry, both of which are expected from a quinonoid deformation on oxidation (Chart II). The RHF/6-31G*-optimized structures for $C_{2 h}$ (anti) and $C_{2 v}$ (syn) 1 have identical heavy-atom bond lengths. The agreement with the apparently anti structure found in the X-ray analysis of the crystal structure is excellent.

Table II shows the calculated HF and MP2 energies for 1 and $1^{\bullet+}$. The latter shows far stronger quinonoid deformations at 6-31 G* than with AM1. The two alternative structures for 1 have essentially the same energies. The $C_{2 h}$ isomer is preferred by $0.13 \mathrm{kcal} \mathrm{mol}^{-1}$ at RHF $/ 6-31 \mathrm{G}^{*}$ and $0.15 \mathrm{kcal} \mathrm{mol}^{-1}$ at RMP2/ 6-31G*.

The experimental heat of formation of 1 has been determined for the crystalline phase, but the heat of sublimation has not been determined. Bondi's incremental method ${ }^{37}$ gives a heat of sublimation of $22.4 \mathrm{kcal} \mathrm{mol}^{-1}$, yielding a gas-phase heat of formation of $25.5 \mathrm{kcal} \mathrm{mol}^{-1}$, in fair agreement with the AM1calculated value ( $19.99 \mathrm{kcal} \mathrm{mol}^{-1}$ ). Table I also shows the calculated and experimental ionization potentials of $1-4$. The differences between the two values are small ( 0.13 and 0.33 eV ) for the compounds without $N$-methyl groups, but increase by about 0.2 eV per $\mathrm{NCH}_{3}$ for compounds 2 and 3. These results

[^3]Chart I: Structures of $1-\mathbf{4}^{++a}$


1





4


$4^{+\quad}$
${ }^{a}$ Calculated (left, AM1; right, 6-31G*) and experimental (X-ray in parentheses) ${ }^{29}$ bond lengths in angstroms.
Chart II: Structures of $\mathbf{4}$ and $\mathbf{4}^{++}$


4
reflect the known weakness of AM1 in reproducing alkyl group stabilization of cationic centers. The MP2/6-31G*-calculated ionization potential for $\mathbf{1}$ (Table II) shows a far larger error than the AM1 value (Table I).
The AM1-calculated vertical $\pi \rightarrow \pi^{*}$ excitation energies show excellent agreement with experiment for $1-3$, confirming the good performance of the CI expansion used. The above results led us to conclude that AM1 is capable of describing the basic electronic

characteristics of these $p$-diaminobenzene systems well. The only major weakness lies in the treatment of $\mathrm{NCH}_{3}$ groups, but this has no effect on system 1, which will be discussed in most detail.

Ground-State Complexes. Two types of structures for the complexes between the neutral molecules and their radical cations were found. The T-shaped structures 1a-2a (Chart III) are actually the most stable dimeric radical cation isomers found for 1 and 2. Although the reorganization energy calculated (AM1/

## Chart III: T-Shaped Ground State of 1a



$1 a$
CI) for these complexes is similar to those for $\mathbf{1 b - 4 b}$ (see below), electron transfer in these species involves very extensive molecular movement (the neutral molecule and the cation swap positions). We have therefore restricted our studies to the layered complexes $\mathbf{1 b}-\mathbf{4 b}$, which have symmetrically equivalent diaminobenzene moieties in the electron-transfer transition states (Chart IV).

Complexes 1b-4b, which lie ca. $2.5 \mathrm{kcal} \mathrm{mol}^{-1}$ higher in energy than $1 \mathrm{a}-4 \mathrm{a}$ in the gas phase, are well suited for degenerate electron self-exchange. Their energies are summarized in Table III; their geometries, in Table IV. The distances between ring centers vary between 3.67 and $4.19 \AA$, but there is little apparent correlation between the substitution pattern and the inter-ring distances, which are in any case very soft parameters. Fritz et
al. ${ }^{38}$ found an inter-ring distance of $3.2 \AA$ in the hexafluorophosphate of the bis(naphthalene) radical anion. This distance is significantly shorter than those found here, although we expect the amino groups to lengthen the inter-ring distance in our systems.

The two molecules in the complexes $\mathbf{1 b}-\mathbf{4 b}$ show the typical geometrical characteristics of discrete neutral and radical cation fragments, as shown in Table IV. The Coulson charge distributions (shown in Table VI) also reflect the neutral/cation nature of these complexes.

The complexation energies decrease monotonically with higher substitution of the amino groups. Remarkable is the high complexation energy of $\mathbf{4 b}$ (Chart V), which can be explained by the boat conformation of this structure. In contrast to $\mathbf{1 b} \mathbf{- 3 b}$, in this structure the positive charge of the complex is centered at the exposed amino groups. The majority of the binding energy seems to involve $\mathrm{N}-\mathrm{N}$ odd-electron bonding, which is most effective for unsubstituted amino groups. The boat-like deformations of 4 and $4^{\circ+}$ favor this type of interaction. Such distortions have been noted by Siegel et al. ${ }^{39}$ and Nelsen and Wolff ${ }^{40}$ for 1,3,5-tris(dialkylamino)-2,4,6-trinitrobenzenes. Such deformations, which Siegel has attributed to the effect of a combination of steric repulsions and strong push-pull conjugation, allow close approach ( $3.1 \AA$ ) of the nitrogens at longer ( $3.7 \AA$ ) ring-ring distances (Chart V).

We have also optimized 1b at UHF/6-31G* and find the structure given in Table V. The geometries of the individual molecules resemble those of the monomers closely. The ringring distance at $3.89 \AA$, in excellent agreement with the AM1calculated value of $3.97 \AA$. The UHF/6-31G* complexation energy is calculated to be $-8.6 \mathrm{kcal} \mathrm{mol}^{-1}$, compared with the AM1 value of $-7.1 \mathrm{kcal} \mathrm{mol}^{-1}$. Once again, these results suggest that AM1 is well suited for this problem.

Transition States and Classical Activation Energies. For all systems except 4 the ring-ring distance decreases by $c a .0 .1 \AA$ between the ground-state complex and the transition state. Although these trends are consistent, they have little energetic significance because the potential energy hypersurface is so flat. The ring-methylated compound 4 behaves completely differently, probably because of the unusual bonding in $\mathbf{4 b}$ (see above). The calculated inter-ring distances (measured between the ring centers) for the transition states are all smaller than those derived from experimental data by Grampp et al. These experimentally derived values rely, however, on a number of approximations and should not be considered to be more than estimated values.
Table IV shows the most important geometrical parameters for the aromatic moieties in the complexes and the transition states. The changes in charge distribution are shown as selected

Chart IV: Ground State 1b and Transition States $\mathbf{1 c}$ of the Electron-Transfer Complex


Table III: Calculated Energies (kcal mol ${ }^{-1}$ ) and Ring-Ring Distances ( $\AA$ ) for Complexes $\mathbf{1 b}-4 \mathrm{c}$

| system | NIMAG ${ }^{\text {a }}$ | $\mathrm{PG}^{\text {b }}$ | $\Delta H_{f}$ | $R_{\text {calc }}{ }^{\text {c }}$ | $R_{\text {exp }}{ }^{\text {c,d }}$ | $\Delta H_{\mathrm{pix}}{ }^{\text {e }}$ | $\Delta H^{*}$ calc | $\Delta H^{*}$ exp | $V_{12}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 b | 0 | $C_{2 v}$ | 194.28 | 3.97 |  | -7.14 |  |  |  |
| 1 c | 1 | $D_{2 h}$ | 204.99 | 3.87 | 4.6 |  | 10.71 | 3.13 | 1.65 |
| 2b | 0 | $C_{1}$ | 212.85 | 4.19 |  | -5.78 |  |  |  |
| 2c | 1 | $C_{2}$ | 223.23 | 4.12 | 5.1 |  | 10.38 | 2.94 | 0.44 |
| 3b | 0 | $C_{2}$ | 231.70 | 4.13 |  | $-4.84$ |  |  |  |
| 3 c | ? | $D_{2}$ | 241.53 | 4.07 | 6.8 |  | 9.83 | 2.77 | 0.50 |
| 4 b | 0 | $C_{2}$ | 145.32 | 3.67 |  | -8.27 |  |  |  |
| 4 c | 1 | $D_{2}$ | 158.36 | 4.10 | 5.1 |  | 13.04 | 2.63 | 1.05 |

${ }^{a}$ Number of imaginary normal vibrations. ${ }^{b}$ Molecular point group. ${ }^{c}$ Ring-center to ring-center distance. ${ }^{d}$ G. Grampp, private communication. ${ }^{e}$ Heat of complexation. The numerical second-derivative calculation actually gives two negative eigenvalues for this structure. This is, however, caused by state-switching during the finite step calculations. We assume that 3 c is the correct transition state by analogy with the other systems.

Table IV: Selected Geometrical Parameters (AM1) of $\mathbf{1 b}-\mathbf{4 c}$ ( $\AA$ and deg)

| parameter | 1b | 1c | 2 b | 2c | 3b | 3c | 4b | 4 c |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bond Lengths |  |  |  |  |  |  |  |  |
| $\mathrm{C}_{1} \mathrm{~N}_{1}$ | 1.412 | 1.369 | 1.420 | 1.378 | 1.420 | 1.379 | 1.415 | 1.373 |
| $\mathrm{C}_{1} \mathbf{N}_{1}{ }^{\prime}$ | 1.344 | 1.369 | 1.357 | 1.378 | 1.358 | 1.379 | 1.348 | 1.373 |
| $\mathrm{C}_{4} \mathrm{~N}_{2}$ | 1.412 | 1.369 | 1.411 | 1.374 | 1.420 | 1.379 | 1.415 | 1.373 |
| $\mathrm{C}_{4} \mathrm{~N}_{2}{ }^{\prime}$ | 1.344 | 1.369 | 1.347 | 1.374 | 1.358 | 1.379 | 1.348 | 1.373 |
| $\mathrm{C}_{1} \mathrm{C}_{2}$ | 1.412 | 1.429 | 1.413 | 1.431 | 1.413 | 1.429 | 1.418 | 1.435 |
| $\mathrm{C}_{1} \mathrm{C}_{2}{ }^{\prime}$ | 1.447 | 1.429 | 1.446 | 1.431 | 1.444 | 1.429 | 1.453 | 1.435 |
| $\mathrm{C}_{4} \mathrm{C}_{4}$ | 1.412 | 1.429 | 1.410 | 1.426 | 1.413 | 1.429 | 1.420 | 1.435 |
| $\mathrm{C}_{3} \mathrm{C}_{4}{ }^{\prime}$ | 1.447 | 1.429 | 1.442 | 1.426 | 1.444 | 1.429 | 1.453 | 1.435 |
| $\mathrm{C}_{2} \mathrm{C}_{3}$ | 1.389 | 1.376 | 1.388 | 1.376 | 1.389 | 1.377 | 1.401 | 1.389 |
| $\mathrm{C}_{2}{ }^{\prime} \mathrm{C}_{3}{ }^{\prime}$ | 1.363 | 1.376 | 1.364 | 1.376 | 1.364 | 1.377 | 1.375 | 1.389 |
|  |  |  |  |  |  |  |  |  |
| $\mathrm{N}_{1} \mathrm{C}_{1} \mathrm{R}_{\mathrm{p}}{ }^{\text {a }}$ b | 6.219 | 1.339 | 5.090 | 0.126 | 5.140 | 0.402 | 7.677 | 3.175 |
| $\mathrm{N}_{1}{ }^{\prime} \mathrm{C}_{1}{ }^{\prime} \mathrm{R}_{\mathrm{p}}{ }^{\prime}$ | -2.174 | -1.339 | -0.798 | -0.120 | -0.336 | $-0.402$ | -17.433 | -3.175 |
| $\mathrm{N}_{2} \mathrm{C}_{4} \mathrm{R}_{\mathrm{p}}$ | 6.219 | 1.339 | 4.837 | 1.835 | 5.140 | 0.402 | 7.677 | 3.175 |
| $\mathrm{N}_{2}{ }^{\prime} \mathrm{C}_{4} \mathrm{R}_{\mathrm{p}}{ }^{\prime}$ | -2.174 | -1.339 | -0.594 | -1.835 | $-0.336$ | -0.402 | -17.433 | -3.175 |
| Dihedral Angles |  |  |  |  |  |  |  |  |
| $S^{b, c} \mathrm{~N}_{1} \mathrm{C}_{1} \mathrm{C}_{2}$ | 150.34 | 167.25 | 156.90 | $176.95$ | 158.36 | 176.96 | 142.29 | 169.73 |
| $\mathrm{S}^{\prime} \mathrm{N}_{1}{ }^{\prime} \mathrm{C}_{1}{ }^{\prime} \mathrm{C}_{2}^{\prime}$ | -175.18 | -167.25 | -175.46 | -176.95 | -176.94 | -176.96 | -171.21 | -169.72 |
| $\mathrm{SN}_{2} \mathrm{C}_{4} \mathrm{C}_{3}$ | 150.34 | 167.25 | 150.46 | 163.41 | 158.36 | 176.96 | 158.12 | 162.53 |
| $\mathrm{S}^{\prime} \mathrm{N}_{2}{ }^{\prime} \mathrm{C}_{4} \mathrm{C}_{3}{ }^{\prime}$ | -175.18 | -167.25 | -176.10 | -163.41 | -176.94 | -176.96 | -171.68 | -162.53 |

${ }^{a} \mathrm{R}_{\mathrm{p}}$ symbolizes the ring plane. ${ }^{b}$ The sign of the angle indicates the direction relative to the ring plane. ${ }^{c} \mathrm{~S}$ symbolizes the atom next to the nitrogen atom, H for $\mathbf{1 b}, \mathbf{c}, \mathbf{2 b}, \mathrm{c}$, and $\mathbf{4 b}, \mathrm{c}$ and C for $\mathbf{2 b}, \mathrm{c}$ and $\mathbf{3 b}, \mathrm{c}$ (Chart I).

Table V: Selected Geometrical Parameters (6-31G*) of $\mathbf{1 b}$ and $\mathbf{1 c}$ ( $\AA$ and deg)

| parameter | 1b | 1c | parameter | 1b | 1c |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Bond Lengths |  |  | Bond Angles |  |  |
| $\mathrm{C}_{1} \mathrm{~N}_{1}$ | 1.411 | 1.360 | $\mathrm{N}_{1} \mathrm{C}_{1} \mathrm{R}_{\mathrm{p}}{ }^{\text {a }}$ b | 2.995 | 0.298 |
| $\mathrm{C}_{1}{ }^{\prime} \mathrm{N}_{1}{ }^{\prime}$ | 1.328 | 1.360 | $\mathrm{N}_{1}{ }^{\prime} \mathrm{C}_{1}{ }^{\prime} \mathrm{R}_{\mathrm{p}}{ }^{\prime}$ | -1.586 | -0.298 |
| $\mathrm{C}_{4} \mathrm{~N}_{2}$ | 1.411 | 1.360 | $\mathrm{N}_{2} \mathrm{C}_{4} \mathrm{R}_{\mathrm{p}}$ | 2.995 | 0.298 |
| $\mathrm{C}_{4}{ }^{\prime} \mathrm{N}_{2}{ }^{\prime}$ | 1.328 | 1.360 | $\mathrm{N}_{2}{ }^{\prime} \mathrm{C}_{4}{ }^{\prime} \mathrm{R}_{\mathrm{p}}{ }^{\prime}$ | -1.586 | -0.298 |
| $\mathrm{C}_{1} \mathrm{C}_{2}$ | 1.390 | 1.409 | Dihedral Angles |  |  |
| $\mathrm{C}_{1}{ }^{\prime} \mathrm{C}_{2}{ }^{\prime}$ | 1.425 | 1.409 |  |  |  |
| $\mathrm{C}_{3} \mathrm{C}_{4}$ | 1.390 | 1.409 | $\mathrm{H}^{b} \mathrm{~N}_{1} \mathrm{C}_{1} \mathrm{C}_{2}{ }^{\prime} \mathrm{N}^{\prime} \mathrm{C}_{1}^{\prime} \mathrm{C}^{\prime}$ | 151.40 | 163.96 -16396 |
| $\mathrm{C}_{3}{ }^{\prime} \mathrm{C}_{4}{ }^{\prime}$ | 1.425 | 1.409 | $\mathrm{H}^{\prime} \mathrm{N}_{1}{ }^{\prime} \mathrm{C}_{1}{ }^{\prime} \mathrm{C}_{2}{ }^{\prime}$ | 188.04 | -163.96 |
| $\mathrm{C}_{2} \mathrm{C}_{3}$ | 1.384 | 1.367 | $\mathrm{HN}_{2} \mathrm{C}_{4} \mathrm{C}_{3}$ | 151.40 | 163.96 -163.96 |
| $\mathrm{C}_{2}{ }^{\prime} \mathrm{C}_{3}{ }^{\prime}$ | 1.350 | 1.367 | $\begin{aligned} & \mathrm{H}^{\prime} \mathrm{N}_{2}^{\prime} \mathrm{C}_{4}^{\prime} \mathrm{C}_{3}{ }^{\prime} \\ & \text { ring-ring } \end{aligned}$ | $\begin{gathered} 188.04 \\ 3.890 \end{gathered}$ | $\begin{array}{r} -163.96 \\ 3.577 \end{array}$ |

${ }^{a} \mathrm{R}_{\mathrm{p}}$ symbolizes the ring plane. ${ }^{b}$ The sign of the angle indicates the direction relative to the ring plane.
net atomic charges in Table VI. The trends in the calculated classical activation energies of the electron-transfer reactions of the unsymmetrical Ar:Ar"+ complexes 1b-3b agree well with experiment (Table III), although the calculated values are all much larger than the experimental enthalpies of activation.

The UHF $/ 6-31 \mathrm{G}^{*}$ structure for the transition state 1 c , shown in Table V , has a ring-ring distance of $3.58 \AA, 0.31 \AA$ shorter than in the complex 1b. The ab initio results therefore confirm

[^4]the shortening of this distance between the minimum and the transition state. The UHF/6-31 G* activation energy, 15.1 kcal $\mathrm{mol}^{-1}$, is even higher than that ( $10.7 \mathrm{kcal} \mathrm{mol}^{-1}$ ) given by AM1. Note that UMP2 cannot be applied to 1c because the UHF wave function is not stable toward symmetry lowering.

We note here that we also located AM1 electron-transfer transition states with $C_{2 h}$ symmetry for 1 and 2 . In these structures, the two rings are translated by about $2.4 \AA$ relative to each other. These structures are, however, less stable than the transition states $\mathbf{1 c}$ and $\mathbf{2 c}$ and represent extremely shallow saddle points that are probably an artifact of the AM1/half-electron method. We have not considered them further.

The Nature of the Hypersurface. Both complexes $\mathbf{1 b}-\mathbf{4 b}$ and the transition states $1 \mathrm{c}-4 \mathrm{c}$ have very flat potential energy hypersurfaces for the degrees of freedom governing the relative positions of the two molecules. This is demonstrated for $1 \mathbf{c}$ in the contour diagram shown in Figure 1. If we assume an arbitrary energy limit of $0.5 \mathrm{kcal} \mathrm{mol}^{-1}$ for energetically accessible structures ( $R T=0.58 \mathrm{kcal} \mathrm{mol}^{-1}$ at 293 K ), the limits for the inter-ring distances are 3.55 and $4.95 \AA$ in the parallel $\left(\theta=180^{\circ}\right)$ orientation and 4.0 and $4.38 \AA$ in the less favorable perpendicular $\left(\theta=90^{\circ}\right)$ orientation. Calculated zero-point energies (ZPEs) also remain constant within these ranges. Grampp et al.'s experimentally derived value lies at the high end of this range. It is, however, clear that electron transfer can occur at a very large range of intermolecular structures.

## Discussion

The Internal Reorganization Energy, $\lambda_{1}$. The reorganization energy, $\lambda$, is split into inner ( $\lambda_{i}$ ) and outer ( $\lambda_{0}$ ) components for weakly coupled systems in Marcus theory. ${ }^{5}$ Weakly coupled in this context refers to the interaction between the reactants. Our system therefore corresponds to the Marcus "inner" reorganization

Table VI: Selected AM1 Coulson Net Atomic Charges of $\mathbf{1 b}-\mathbf{4 c}$

| atom | 1 b | 1 c | 2b | 2c | 3b | 3c | 4b | 4 c |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{N}_{1}$ | -0.315 | -0.322 | -0.241 | -0.222 | -0.249 | -0.233 | -0.324 | -0.325 |
| $N_{1}{ }^{\prime}$ | -0.251 | -0.322 | -0.138 | -0.222 | -0.159 | -0.233 | -0.250 | -0.325 |
| $N_{2}$ | -0.315 | -0.322 | -0.314 | -0.322 | -0.249 | -0.233 | -0.324 | -0.325 |
| $\mathrm{N}_{2}{ }^{\prime}$ | -0.251 | -0.322 | -0.265 | -0.322 | -0.159 | -0.233 | -0.250 | -0.325 |
| $\mathrm{C}_{1}$ | -0.008 | 0.092 | 0.017 | 0.087 | 0.007 | 0.086 | -0.008 | 0.100 |
| $\mathrm{C}_{1}{ }^{\prime}$ | 0.144 | 0.092 | 0.105 | 0.087 | 0.104 | 0.086 | 0.150 | 0.100 |
| $\mathrm{C}_{4}$ | $-0.008$ | 0.092 | -0.008 | 0.083 | 0.007 | 0.086 | $-0.008$ | 0.100 |
| $\mathrm{C}_{4}{ }^{\prime}$ | 0.144 | 0.092 | 0.149 | 0.083 | 0.104 | 0.086 | 0.150 | 0.100 |
| $\mathrm{C}_{2}$ | -0.151 | -0.146 | -0.150 | -0.141 | -0.154 | -0.144 | -0.085 | -0.086 |
| $\mathrm{C}_{2}{ }^{\prime}$ | -0.130 | $-0.146$ | -0.115 | -0.141 | -0.133 | -0.146 | -0.074 | -0.084 |
| $\mathrm{C}_{3}$ | -0.151 | $-0.146$ | -0.155 | $-0.150$ | -0.153 | -0.144 | -0.087 | -0.086 |
| $\mathrm{C}_{3}{ }^{\text {' }}$ | $-0.130$ | $-0.146$ | -0.143 | -0.150 | -0.136 | -0.146 | -0.080 | -0.084 |



Figure 1. Heat of formation contour map of the $D_{2}$ hypersurface of 1.
Chart V: AM1-Optimized Structure of $\mathbf{4} \mathbf{b}$


4b
model. The complexes calculated here are clearly strongly coupled, so that the traditional definitions of $\lambda_{i}$ and $\lambda_{0}$ do not apply. Nevertheless, the differences between the behavior predicted for a loosely coupled system and our relatively tight complexes are important, and so we will first consider the magnitude of $\lambda_{i}$, the internal reorganization energy for noncoupled systems.

Both Nelsen et al. ${ }^{12}$ and Grampp et al. ${ }^{13}$ have suggested consistently that $\lambda_{i}$ is significantly larger for organic electrontransfer reactions than has commonly been assumed. Unfortu-

Table VII: Calculated $\Delta H_{j}$ and $\Delta E_{j}$ Values According to Eqs 1 and $2\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$


Figure 2. State energy level diagram for $\mathbf{1 b}$ and 1 c . The values have been determined via a linear synchronous transit calculation.
nately, direct AM1 calculations of $\lambda_{\mathrm{i}}$ for 1,4-bis(dimethylamino)benzene (3) and its radical cation contained an error, ${ }^{12}$ so that the published values are far too low. Goez ${ }^{20}$ estimated $\lambda_{i}$ for 2 and 3 to be 3.8 and $4.4 \mathrm{kcal} \mathrm{mol}^{-1}$, respectively. We find these values to be far too low. Our calculated $\lambda_{1}$ values are extremely large, but cannot be grossly in error because all the calculational methods used yield similar results. It is extremely unlikely that AM1, UHF/6-31G*, and UMP2/6-31G* all give an order of magnitude error.

The enthalpic component of $\lambda_{i}, \Delta H_{i}$, can be calculated using the nomenclature introduced by Nelsen ${ }^{12}$ as

$$
\begin{equation*}
\Delta H_{\mathrm{i}}=\left[\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{c}^{\circ}\right)-\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{n}^{\circ}\right)\right]+\left[\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{n}^{+}\right)-\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{c}^{+}\right)\right] \tag{1}
\end{equation*}
$$

for the AM1 results or, using total energies for the ab initio methods,

$$
\begin{equation*}
\Delta E_{\mathrm{i}}=\left[E\left(\mathrm{c}^{\circ}\right)-E\left(\mathrm{n}^{\circ}\right)\right]+\left[E\left(\mathrm{n}^{+}\right)-E\left(\mathrm{c}^{+}\right)\right] \tag{2}
\end{equation*}
$$

where (c) and ( n ) indicate the geometry (that of the cation or neutral species, respectively) and the superscripts ( ${ }^{\circ}$ ) and ( ${ }^{+}$) indicate the charge on the species calculated. ${ }^{12}$ Table VII shows the results obtained. The "least reliable" calculational method (AM1) yields the lowest $\Delta H_{\mathrm{i}}$ value for 1 , but the agreement between AM1 and MP2/6-31G* is good, so that we conclude that $\Delta H_{\mathrm{i}}$ (or $\Delta E_{\mathrm{i}}$ ) for $\mathbf{1} / \mathbf{1}^{\bullet+}$ is about $23-27 \mathrm{kcal} \mathrm{mol}^{-1}$. If $\lambda_{\mathrm{i}}$ is

Table VIII Correlation between the Normal Vibrations of $\mathbf{1 b}$ and $1 \mathbf{c}$

| Irreducible Representations |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1b ( $C_{20}$ ) |  |  | 1c ( $D_{2 h}$ ) | 1b ( $C_{2 v}$ ) |  | 1c ( $D_{2 h}$ ) |  |  |
|  |  | $\begin{aligned} & a_{1} \\ & a_{2} \end{aligned}$ | $\vec{\rightarrow}$ | $\begin{aligned} & a_{\mathrm{g},}, b_{2 u} \\ & a_{u}, b_{2 g} \end{aligned}$ | $\begin{aligned} & \overline{b_{1}} \\ & b_{2} \end{aligned}$ | $\rightarrow$ |  |  |  |
| Normal Vibrations |  |  |  |  |  |  |  |  |  |
| 1b ( $C_{2 v}$ ) | $\mathrm{cm}^{-1}$ | 1c $\left(D_{2 h}\right)$ | $\mathrm{cm}^{-1}$ | shift ( $\left.\mathrm{cm}^{-1}\right)^{a}$ | $1 \mathrm{l}\left(C_{20}\right)$ | $\mathrm{cm}^{-1}$ | 1c ( $D_{2 h}$ ) | $\mathrm{cm}^{-1}$ | shift ( $\left.\mathrm{cm}^{-1}\right)^{a}$ |
| $1 \mathrm{~b}_{2}$ | 30.3 | $1 \mathrm{~b}_{3}$ | 26.9 | -3.4 | $9 \mathrm{~b}_{1}$ | 1093.4 | $5 \mathrm{~b}_{3 \mathrm{~g}}$ | 1109.0 | +15.6 |
| $2 \mathrm{~b}_{2}$ | 35.1 | $1 \mathrm{~b}_{1 \mathrm{~g}}$ | 29.0 | -6.1 | $12 \mathrm{a}_{2}$ | 1133.7 | $7 \mathrm{a}_{4}$ | 1153.2 | +19.5 |
| $1 a_{1}$ | 42.3 | $1 \mathrm{a}_{\mathrm{g}}$ | 33.5 | -8.8 | $14 \mathrm{~b}_{2}$ | 1141.0 | $7 \mathrm{~b}_{1 \mathrm{~g}}$ | 1117.1 | -23.9 |
| $1 \mathrm{a}_{2}$ | 50.7 | $1 a_{u}$ | 22.8 | -27.9 | $10 b_{1}$ | 1145.2 | $5 \mathrm{~b}_{1 u}$ | 1109.0 | -36.2 |
| $1 \mathrm{~b}_{1}$ | 54.2 | $1 \mathrm{~b}_{3 \mathrm{~g}}$ | 29.9 | -24.3 | $13 a_{2}$ | 1222.6 | $6 b_{2 g}$ | 1154.0 | -68.6 |
| $2 \mathrm{~b}_{1}$ | 68.8 | $1 b_{l u}$ | 60.3 | -8.5 | $11 \mathrm{~b}_{1}$ | 1232.6 | $6 b_{3 g}$ | 1232.7 | +0.1 |
| $2 a_{1}$ | 104.4 | $2 \mathrm{~b}_{2 \mathrm{u}}$ | 113.5 | +9.1 | $12 \mathrm{~b}_{1}$ | 1251.2 | $6 b_{1 u}$ | 1233.0 | -18.2 |
| $3 a_{1}$ | 139.3 | $2 \mathrm{ag}_{\mathrm{g}}$ | 120.6 | -18.7 | $14 a_{1}$ | 1272.8 | $7 \mathrm{~b}_{2 \mathrm{u}}$ | 1219.7 | -53.1 |
| $3 \mathrm{~b}_{2}$ | 278.7 | $2 \mathrm{~b}_{1 \mathrm{~g}}$ | 257.8 | -20.9 | $15 a_{1}$ | 1277.4 | $8 \mathrm{a}_{\mathrm{g}}$ | 1273.1 | -4.3 |
| $2 \mathrm{a}_{2}$ | 287.2 | $2 a_{u}$ | 348.9 | +61.7 | $14 a_{2}$ | 1354.4 | $8 \mathrm{a}_{u}$ | 1355.8 | +1.4 |
| $3 \mathrm{~b}_{1}$ | 291.8 | $2 \mathrm{~b}_{3 \mathrm{~g}}$ | 381.7 | +89.9 | $15 \mathrm{a}_{2}$ | 1364.3 | $7 \mathrm{~b}_{2 \mathrm{~g}}$ | 1356.7 | -8.1 |
| $4 \mathrm{~b}_{2}$ | 344.4 | $2 \mathrm{~b}_{3}$ | 309.7 | -34.7 | $13 \mathrm{~b}_{1}$ | 1385.4 | $7 \mathrm{~b}_{3 \mathrm{~g}}$ | 1476.5 | +91.1 |
| $3 a_{2}$ | 348.5 | $1 \mathrm{~b}_{2 \mathrm{~g}}$ | 355.7 | +7.2 | $15 b_{2}$ | 1392.6 | $8 \mathrm{~b}_{1 \mathrm{~g}}$ | 1410.1 | +17.5 |
| $4 a_{2}$ | 376.9 | $3 a_{u}$ | 421.3 | +44.4 | $16 b_{2}$ | 1404.7 | $8 \mathrm{~b}_{1 \mathrm{~g}}$ | 1410.2 | +5.5 |
| $4 \mathrm{~b}_{1}$ | 380.6 | $2 \mathrm{~b}_{1 \mathrm{u}}$ | 382.0 | +1.4 | $14 \mathrm{~b}_{1}$ | 1504.0 | $7 \mathrm{~b}_{14}$ | 1473.6 | -30.4 |
| $5 \mathrm{~b}_{1}$ | 387.7 | $3 b_{3 g}$ | 404.4 | +16.7 | $16 a_{2}$ | 1589.6 | $8 \mathrm{~b}_{2 \mathrm{~g}}$ | 1657.9 | +68.3 |
| $4 a_{1}$ | 491.4 | 3 ag | 481.1 | -10.3 | $15 b_{1}$ | 1592.8 | $8 \mathrm{~b}_{1 u}$ | 1614.1 | +21.3 |
| $6 b_{1}$ | 495.9 | $2 b_{1 u}$ | 420.5 | -75.4 | $16 a_{1}$ | 1634.3 | $8 \mathrm{~b}_{2 u}$ | 1293.5 | -340.8* |
| $5{ }^{2}$ | 498.9 | $2 \mathrm{~b}_{2 \mathrm{~g}}$ | 430.9 | -68.0 | $16 b_{1}$ | 1679.4 | $8 \mathrm{~b}_{1 u}$ | 1614.5 | -64.9 |
| ${ }_{5} a_{2}$ | 503.6 | $4 a_{u}$ | 499.0 | -4.6 | $17 a_{1}$ | 1680.8 | $9 \mathrm{a}_{8}$ | 1660.9 | -19.9 |
| $5 \mathrm{a}_{1}$ | 515.4 | $3 \mathrm{~b}_{2 \mathrm{u}}$ | 491.3 | -24.1 | $17 \mathrm{~b}_{2}$ | 1682.3 | $8 \mathrm{~b}_{3 \mathrm{u}}$ | 1687.7 | +5.4 |
| $7 a_{2}$ | 516.7 | $4 \mathrm{ag}_{\mathrm{g}}$ | 499.2 | -17.5 | $18 \mathrm{~b}_{2}$ | 1684.4 | $9 \mathrm{~b}_{1 \mathrm{~g}}$ | 1683.4 | -1.0 |
| $6 a_{1}$ | 543.8 | $4 \mathrm{a}_{\mathrm{g}}$ | 508.2 | -35.6 | $19 b_{2}$ | 1741.1 | $9 b_{3 u}$ | 1661.1 | -80.0 |
| $7 a_{1}$ | 557.4 | $4 \mathrm{~b}_{2 \mathrm{u}}$ | 518.4 | -39.0 | $17 \mathrm{a}_{2}$ | 1745.0 | $9 a_{u}$ | 1659.6 | -85.4 |
| $5 \mathrm{~b}_{2}$ | 607.7 | $3 \mathrm{~b}_{1 \mathrm{~g}}$ | 323.7 | $-284.0^{*}$ | $18 a_{1}$ | 1773.4 | $9 b_{2 u}$ | 1669.1 | -104.3 |
| $8 a_{1}$ | 628.3 | $1 \mathrm{~b}_{2 \mathrm{u}}$ | -1052.0 | -628.3 ** | $20 \mathrm{~b}_{2}$ | 1780.5 | $10 \mathrm{~b}_{1 \mathrm{~g}}$ | 1738.3 | -42.2 |
| $8 \mathrm{a}_{2}$ | 667.2 | $5 \mathrm{au}_{4}$ | 674.9 | +7.7 | $19 a_{1}$ | 1822.1 | $11 a_{8}$ | 1809.8 | -12.3 |
| $6 b_{2}$ | 676.5 | $3 b_{3 u}$ | 465.9 | -210.6* | $20 a_{1}$ | 1862.9 | $10 \mathrm{~b}_{2 \mathrm{u}}$ | 1736.1 | -126.8* |
| $9 a_{2}$ | 684.0 | $4 \mathrm{~b}_{2 \mathrm{~g}}$ | 675.2 | -8.8 | $21 a_{1}$ | 1885.4 | $10 a_{8}$ | 1736.6 | $-148.8{ }^{*}$ |
| $7 \mathrm{~b}_{2}$ | 710.8 | $4 \mathrm{~b}_{3 \mathrm{u}}$ | 688.7 | -22.1 | $18 \mathrm{a}_{2}$ | 3144.5 | $10 a_{u}$ | 3161.7 | +17.2 |
| $8 \mathrm{~b}_{2}$ | 839.9 | $4 \mathrm{~b}_{1 \mathrm{~g}}$ | 689.6 | -150.3* | $21 \mathrm{~b}_{2}$ | 3149.8 | $11 \mathrm{~b}_{1 \mathrm{~g}}$ | 3164.9 | +15.1 |
| $7 \mathrm{~b}_{1}$ | 856.3 | $4 \mathrm{~b}_{3 \mathrm{~g}}$ | 858.5 | +2.2 | $17 \mathrm{~b}_{1}$ | 3152.1 | $9 \mathrm{~b}_{3 \mathrm{~g}}$ | 3171.7 | +19.6 |
| $9 b_{2}$ | 868.0 | $5 \mathrm{~b}_{3 \mathrm{u}}$ | 873.6 | +5.6 | $19 a_{2}$ | 3173.8 | $9 \mathrm{~b}_{3 \mathrm{~g}}$ | 3162.0 | -11.8 |
| $8 b_{1}$ | 883.1 | $4 \mathrm{~b}_{1 u}$ | 865.4 | -17.7 | $22 \mathrm{~b}_{2}$ | 3175.4 | $11 \mathrm{~b}_{3 \mathrm{u}}$ | 3165.1 | -10.3 |
| $9 a_{1}$ | 894.6 | $5 \mathrm{~b}_{2 \mathrm{u}}$ | 851.9 | -42.7 | $22 a_{1}$ | 3176.5 | $11 \mathrm{~b}_{2 u}$ | 3058.8 | -117.7 |
| $10 a_{1}$ | 909.4 | $5 \mathrm{ag}_{\mathrm{g}}$ | 542.9 | -366.5** | $18 \mathrm{~b}_{1}$ | 3181.5 | $9 b_{1 u}$ | 3172.1 | -9.4 |
| $10 \mathrm{~b}_{2}$ | 921.4 | $5 \mathrm{~b}_{1 \mathrm{~g}}$ | 873.7 | -47.7 | $23 a_{1}$ | 3221.3 | $12 \mathrm{a}_{8}$ | 3177.7 | -43.6 |
| $11 \mathrm{~b}_{2}$ | 979.7 | $6 \mathrm{~b}_{3 \mathrm{u}}$ | 974.1 | -5.6 | $20 a_{2}$ | 3416.4 | $11 a_{u}$ | 3486.9 | +70.5 |
| $10 a_{2}$ | 980.1 | $6 \mathrm{au}^{\text {a }}$ | 972.9 | -7.2 | $19 \mathrm{~b}_{1}$ | 3416.5 | $10 \mathrm{~b}_{3 \mathrm{~g}}$ | 3486.1 | +69.6 |
| $11 a_{2}$ | 983.2 | $5 \mathrm{~b}_{2 \mathrm{~g}}$ | 975.0 | -8.2 | $20 \mathrm{~b}_{1}$ | 3438.3 | $10 b_{1 u}$ | 3487.1 | +48.8 |
| $11 a_{1}$ | 988.3 | $6 \mathrm{ag}_{\mathrm{g}}$ | 886.4 | -101.9 | $21 a_{2}$ | 3449.3 | $10 \mathrm{~b}_{2 \mathrm{~g}}$ | 3488.1 | +38.8 |
| $12 \mathrm{~b}_{2}$ | 993.2 | $6 \mathrm{~b}_{1 \mathrm{~g}}$ | 971.4 | -21.8 | $23 \mathrm{~b}_{2}$ | 3459.1 | 12 blg | 3500.2 | +41.1 |
| $12 a_{1}$ | 1024.4 | $6 b_{2 u}$ | 995.5 | -28.9 | $24 \mathrm{~b}_{2}$ | 3459.9 | $12 \mathrm{~b}_{3 \mathrm{u}}$ | 3501.8 | +41.9 |
| $13 a_{1}$ | 1063.5 | $7 \mathrm{a}_{\mathrm{g}}$ | 1043.0 | -20.5 | $24 \mathrm{a}_{1}$ | 3485.5 | $12 \mathrm{~b}_{2 \mathrm{u}}$ | 3428.2 | -57.3 |
| $13 \mathrm{~b}_{2}$ | 1090.4 | $7 \mathrm{~b}_{3 \mathrm{u}}$ | 1116.8 | +26.4 | $25 \mathrm{a}_{1}$ | 3488.0 | $13 \mathrm{ag}_{\mathrm{g}}$ | 3508.5 | +20.5 |
|  |  |  |  |  |  | total (hydro | stretches) |  | +133.0 |

${ }^{a}\left({ }^{*}\right)$ Vibrations with large shifts (shown in Figure 3). **The imaginary vibration in 1c.
similar in magnitude, these results are inconsistent with the observed low activation energies in acetonitrile if the harmonic approximation is valid. ${ }^{13}$ Note that the trends observed above in the complexation energies are reversed for $\Delta H_{\mathrm{i}}$ (i.e. $\Delta H_{\mathrm{i}}$ increases monotonically with higher substitution of the amino groups).
Reorganization Energies in Precursor Complexes, $\lambda_{\mathrm{lc}}$. Because of the tight coupling in our calculated complexes, we define a quantity, $\lambda_{\mathrm{ic}}$, that represents the reorganization energy (without any solvent contribution) within the precursor complexes. As shown below, this quantity differs considerably from $\lambda_{i}$ in a manner that depends directly on the complexation energy. Figure 2 shows the AM1 CI-calculated state energy level diagram for a linear synchronous reaction path (LST) ${ }^{41}$ for the self-exchange process in $1 / 1^{\bullet+}$. This curve reveals a further component of $\lambda_{\mathrm{ic}}$. If we consider the complexation energy as a resonance energy between two hypothetical "no bond resonance" states, as appears reasonable

[^5]from the behavior of odd-electron bonds ${ }^{42}$,
$$
11^{\bullet+} \leftrightarrow 1^{\circ+} 1
$$
the ground state is stabilized by the complexation energy and the first excited state is destabilized by about the same amount. The resulting expression for the reorganization enthalpy in the complex, $\Delta H_{\text {ic }}$, is
\[

$$
\begin{align*}
\Delta H_{\mathrm{ic}}=\left[\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{c}^{\circ}\right)-\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{n}^{\circ}\right)\right]+\left[\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{n}^{+}\right)-\right. \\
\left.\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{c}^{+}\right)\right]-2 \Delta H_{\mathrm{cplx}} \tag{3}
\end{align*}
$$
\]

where $\Delta H_{\text {cplx }}$ is the enthalpy of complexation:

$$
\begin{equation*}
\Delta H_{\mathrm{cplx}}=\Delta H_{\mathrm{f}}^{\circ}\left(\mathbf{1}: 1^{\bullet+}\right)-\Delta H_{\mathrm{f}}^{\circ}(\mathbf{1})-\Delta H_{\mathrm{f}}^{\circ}\left(\mathbf{1}^{\bullet+}\right) \tag{4}
\end{equation*}
$$

Equation 3 gives a calculated value of $36.7 \mathrm{kcal} \mathrm{mol}^{-1}$ for $\Delta H_{\mathrm{ic}}$, compared with the value of $42.7 \mathrm{kcal} \mathrm{mol}^{-1}$ given by the state-


Figure 3. Correlated vibrations of $\mathbf{1 b}$ and $\mathbf{1 c}$ that are largely responsible for the change in the ZPE.


Figure 4. Thermodynamic activation parameters of $\mathbf{1 c}$ as a function of temperature.
splitting using AMI/CI. Equation 3 therefore gives a realistic estimate of $\Delta H_{\text {ic }}$ as we have defined it. Note that traditional Marcus theory for bimolecular processes involves a work term to bring the molecules together to form the precursor complex. ${ }^{43}$ This work term is clearly related to the complexation energy contribution to $\lambda_{i c}$. The above discussion (and eqs 3 and 4 ) assumes that $\Delta H_{\mathrm{i}}$ remains constant in the complex. This assumption seems realistic when the very small geometrical changes between isolated reactants and the individual components of the complex are considered. Note that eq 3 predicts an increase in $\Delta H_{\text {ic }}$ with increasing complexation energy. If the harmonic approximation ( $\Delta H^{*}=\Delta H_{\text {ic }} / 4$ ) applies, this results in an increase in the classical activation energy of $\Delta H_{\text {cplx }} / 2$ for the activation energy relative to the separated reactants. Note that these trends are opposite to what one might expect because the coupling in the complex is much stronger than that in the transition state.

The Classical Activation Energy. The parabolas assumed by Marcus theory (dotted curves) superimposed on Figure 2 deviate moderately from the calculated linear synchronous transit energies. The calculated activation energy ( $10.7 \mathrm{kcal} \mathrm{mol}^{-1}$ ) is significantly larger than $\lambda_{\mathrm{ic}} / 4\left(9.4 \mathrm{kcal} \mathrm{mol}^{-1}\right)$, especially considering the large $V_{12}$ value ( $1.7 \mathrm{kcal} \mathrm{mol}{ }^{-1}$ ). As discussed above, however, this value is too high to be reconciled with the experimental data. In an attempt to resolve this difference, we have calculated the zero-point vibration energies (ZPEs) for the minimum 1 b and the transistion state $\mathbf{1 c}$. Note that, although AM1-calculated energies are usually described as heats of formation (which contain the ZPE), they are based on total energy calculations on the hypothetical motionless state. It is therefore legitimate to correct the relative energies of isomers because the assumption of equal ZPEs for isomers is inherent in the parametrization.

The calculated (AM1) ZPEs for the minimum and transition state are 174.5 and $168.7 \mathrm{kcal} \mathrm{mol}^{-1}$, respectively, so that the ZPE-corrected activation energy is only $4.91 \mathrm{kcal} \mathrm{mol}^{-1}$, in far better agreement with experiment than the motionless value. A ZPE correction of this magnitude is unprecedented in our experience (it corresponds to the loss of a $4050-\mathrm{cm}^{-1}$ vibration), and so we have correlated and analyzed the normal vibrations of $\mathbf{1 b}$ and 1c. The results are shown in Table VIII for all 90 vibrations and in Figure 3 for the eight vibrations (marked with asterisks in Table VIII) that are largely responsible for the change in ZPE. These vibrations are related to the quinonoid deformation of the ring, the pyramidalization of the nitrogens, and out-of-plane deformations of the ring. There is strong coupling between the latter two types of vibration, so that these vibrations all relate directly to the geometric variation associated with internal reorganization. Marcus theory assumes that the internal reorganization vibrational frequency, $\nu_{n}$, is constant throughout the reaction. In our closely coupled system this is clearly not the

[^6]case, so that we must correct the activation energy in the complex correspondingly:
\[

$$
\begin{equation*}
\Delta H_{\text {ic }}^{\ddagger}=\frac{\lambda_{\text {ic }}}{4}-\sum_{n=1}^{3 N-6} \frac{h \delta \nu_{n}}{2}-V_{12} \tag{5}
\end{equation*}
$$

\]

where $\Delta \nu_{n}$ is the difference between the frequency of the $n^{\text {th }}$ vibration in the precursor complex and the transition state.

Thermodynamics of the Classical Activation Process. The enthalpy and free energy of activation for the classical activation process for self-exchange in $\mathbf{1}$ can be calculated from the AM1 energies, geometries, and vibrational frequencies. The results are shown in Figure 4. Note that these data do not include any correction for heavy-atom tunneling or solvent effects. The enthalpy of activation increases slightly (from 4,92 and 5.53 kcal $\mathrm{mol}^{-1}$ ) between 100 and 400 K . In this range, $\Delta S^{\ddagger}$ increases from 4.3 to $6.6 \mathrm{cal} \mathrm{K}^{-1}$, so that $\Delta G^{*}$ decreases from 4.49 to 2.81 $\mathrm{kcal} \mathrm{mol}^{-1}$. The calculated values for $\Delta H^{*}, \Delta G^{*}$, and $\Delta S^{*}$ at 300 K are 5.26 and $3.45 \mathrm{kcal} \mathrm{mol}^{-1}$ and $6.0 \mathrm{cal} \mathrm{K}^{-1}$, respectively. The thermodynamics calculated here apply to the activation process between the complex and the transistion state. They do not take the softness of both species into account, but should nevertheless provide an indication of the reliability of the calculations.
The Electronic Coupling Matrix Element. Within a two-state model, the splitting between the two electronic states at the transition state is equal to twice the matrix element coupling these two states, $V_{12}$ (Table III). Rather than calculate $V_{12}$ directly, we have calculated the state-splitting at the transistion state using AM1/CI. The magnitude of $V_{12}$ determines whether the reaction proceeds adiabatically ( $V_{12} \geq R T$ ) or nonadiabatically ( $V_{12} \ll R T$ ). ${ }^{5}$ The calculated values for $V_{12}$ at the optimized transistion states (Table III) are smaller than $R T$ ( 0.58 kcal $\mathrm{mol}^{-1}$ ) for 2 c and 4 c , but larger for 1 c and 3 c . These values agree rather well with those of Grampp et al., recalculated from experimental data. Grampp determined $V_{12}$ for $\mathbf{1 c}-4 \mathbf{c}$ as 0,10 , $0.14,0.11$, and $0.14 \mathrm{kcal} \mathrm{mol}^{-1}$. However, at longer distances $V_{12}$ is considerablysmaller. The experimentally determined $V_{12}$ values and inter-ring distances are mutually compatible for an electrontransfer process occurring at larger distances than given by our model.

## Conclusions

The present study underlines the usefulness of semiempirical calculations for studying electron-transfer reactions. The performance of AM1 for this problem shows no significant deviations from the known experimental data.

The calculated (AM1 and MP2/6-31G*) values for $\lambda_{i}$ are larger than have been previously assumed, and the vertical excitation energy calculated for the precursor complexes is even higher. These values would be incompatible with the harmonic ( $\lambda / 4$ ) approximation of Marcus theory were it not for a very large ( $5.8 \mathrm{kcal} \mathrm{mol}^{-1}$ ) lowering of the calculated barrier by the zero-point energy correction.

The calculated activation thermodynamics and magnitude of the electronic matrix coupling element $V_{12}$ are in good agreement with values derived from experiment in solution.

Our calculations therefore suggest strongly that the inner reorganization energy is the major contributor to the activation energy in $p$-diaminobenzene electron-transfer reactions and that the close coupling found for the gas-phase reaction increases the barrier height from the precursor complex but decreases it from the separated reactants. Further studies are needed to confirm the major role played by changes in vibrational frequencies along the reaction path.
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